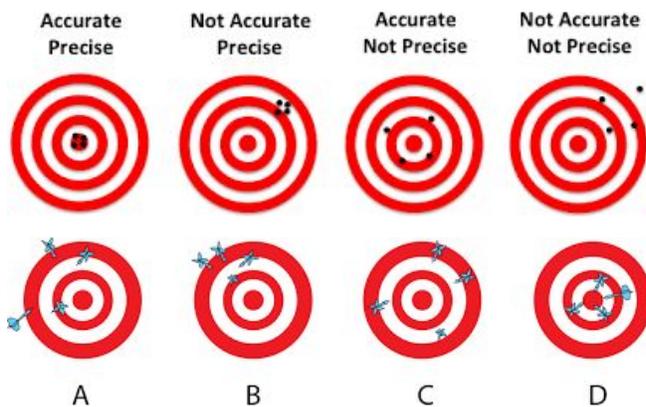


MEASUREMENT AND UNITS

“LORD, make me to know my end, And what is the **measure** of my days,
That I may know how frail I am.” Psalm 39:4

- mathematics: science of quantity; language of science
- equation: set of symbols summarizing mathematical relationship between quantities [$V=lwh$]; most important part of equation is the equal sign; equation may be rearranged to get desired information [$h=V/lw$]
- *Fibonacci numbers*: begins with 0 and 1; every other number in the sequence is found by adding the two numbers before it:
 $0+1=1 \rightarrow 1+1=2 \rightarrow 1+2=3 \rightarrow 2+3=5 \rightarrow 3+5=8 \rightarrow 5+8=13 \rightarrow 8+13=21 \rightarrow 13+21=34$
examples in nature: daisy head has 21 clockwise spirals, 34 counterclockwise spirals
pineapples have 8 curves one way, 13 curves the other way
- Accuracy: how closely a measurement reflects the actual value (dart hitting a target)
Precision: repeatability of a measurement, or how close several measurements are to each other (ability to consistently hit the bullseye of the target)



Significant figures

- used to record only measured values or calculated values (not speculated or hypothetical values)
- all nonzero digits are significant (1,2,3,4,5,6,7,8,9)
- Zeroes before/to the left of first nonzero digit are never significant: 0.0917 = three significant figures
- Zeroes between nonzero digits are always significant: 30.005 = five significant figures
- Zeroes after/to the right of last nonzero digit are significant only if there is a decimal point in the number: 40.0 = three significant figures; 40 = one significant figure

- Calculating with significant figures:
 - multiplication and division: answer rounded to same# of significant figures as least significant factor
Ex: $3.24 \times 0.08 = 0.2592 \rightarrow 0.3$
 - addition and subtraction: results are rounded to the last place value that is significant in the least accurate measurement
Ex: $5.20 + 6 = 11.20 \rightarrow 11$
- Round answers to significant figures only at the end of all calculations to avoid multiple rounding errors*
 [Application p. 15]

Scientific notation

- shortcut to writing extremely large or small numbers
 - based on fact that every number (except 0) can be expressed as a number between 1 and 10 multiplied by a power of 10
Ex: $6,020,000 = 6.02 \times 10^6$ (positive exponent \rightarrow decimal moved from right/large number)
 $0.00092 = 9.2 \times 10^{-4}$ (negative exponent \rightarrow decimal moved from left/small number)
- [Application p.17]

Units

- Measured data must include units for universal understanding; need for developing system of measurement
- Cubit: length of person's arm from elbow to tip of middle finger; based on the individual
 need for developing a standard of measure: specific measure to which other measures are compared to ensure uniformity
- F.P.S. system: system of measurement used in the United States; foot-pound-second system
Unciae: "inches" / mille passus: "thousand double paces" / libra: "weighing balance"
- Metric system:

measurement	unit
length	meter (m)
weight	gram (g) / kilogram (kg)
volume	liter (L) / cubic meter (m ³)
time	second (s)
temperature	celsius (°C)

- Prefix attached to name of each basic unit to make it larger or smaller based on powers of 10:

Prefix	Symbol	Meaning	Power of 10
kilo-	k	1000 x	10^3
deca-	da	10 x	10^1
deci-	d	1/10 x	10^{-1}
centi-	c	1/100 x	10^{-2}
milli-	m	1/1000 x	10^{-3}

- SI: *Système Internationale d'Unités*, universally accepted as standard system of measurement for scientific and technical purposes
[Metric system conversion illustrations p.20]
[Measuring mass illustrations p. 21]
- Temperature conversions between Fahrenheit (F), Celsius (C) and Kelvin (K)
 $F = 9/5 \times ^\circ\text{C} + 32$
 $C = 5/9 (F - 32)$
- The coldest possible temperature is absolute zero: the temperature at which molecular vibrations ceases = 0 K (zero Kelvin)
 $K = ^\circ\text{C} + 273.15$
 $^\circ\text{C} = K - 273.15$
- *memorize boiling point/freezing point of water in K/F/°C
[Application p. 24]

VOLUME AND DENSITY

- mass/weight/volume/density are several physical properties of matter commonly used in physical science

Volume

- Amount of space that matter takes up; describes how large or small an object is
- Geometric formulas can be used to find the volumes of simple shapes
[Table p.26]
 $1 \text{ cm}^3 = 1 \text{ mL}$

[Application p.26]

- The volume of an irregularly shaped solid can be measured using the technique of fluid displacement [demonstration]
-subtracting the initial volume (water only) from the final volume (water+object) gives the volume of the object:

$$V_{(\text{object})} = V_{(\text{final})} - V_{(\text{initial})}$$

- Direct measurement method uses a container with volume markings
-only works with liquid or if the solid is in small pieces that fit together almost perfectly

Density

- Density: amount of matter in a certain volume; how much there is in a certain amount of space
- Density of water = 1 g/cm³
- found by dividing mass by volume:

$$\text{density} = \frac{\text{mass}}{\text{volume}} \quad \text{OR} \quad \rho = \frac{m}{V}$$

Ex: What is the density of a cork cylinder that has a mass of 400.g and takes up a volume of 1700cm³? Is cork more or less dense than water?

- Density can be used to identify substances (gold v. "fools gold")
- The relative densities of two substances will determine whether one will float in the other → in general, a solid will float in a liquid if the solid has a lower density than the liquid

Specific gravity

- Ratio of density of a substance to the density of a standard
- For solids and liquids, the standard is water, which has a density of 1.00 g/cm³
- Found by dividing the density of the substance by the density of water:

$$\text{Specific gravity} = \frac{\rho_{\text{substance}}}{\rho_{\text{water}}}$$

Ex: What is the specific gravity of iron if its density is 7.87g/cm³?

- Note: specific gravity is just a number with NO UNITS